



# Superconductivity induced spectral weight redistribution in cuprate high temperature superconductors



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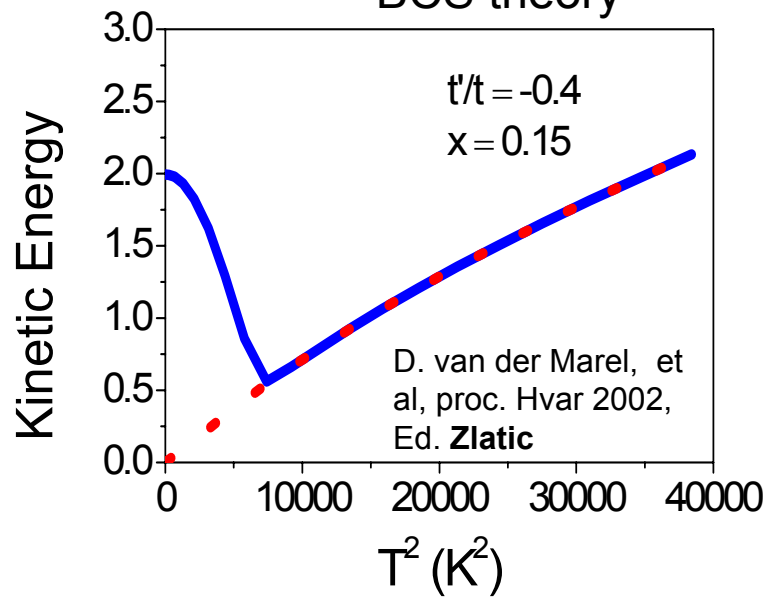
# Optical study of spectral weight transfer in relation to the kinetic changes of the normal and the superconducting state.



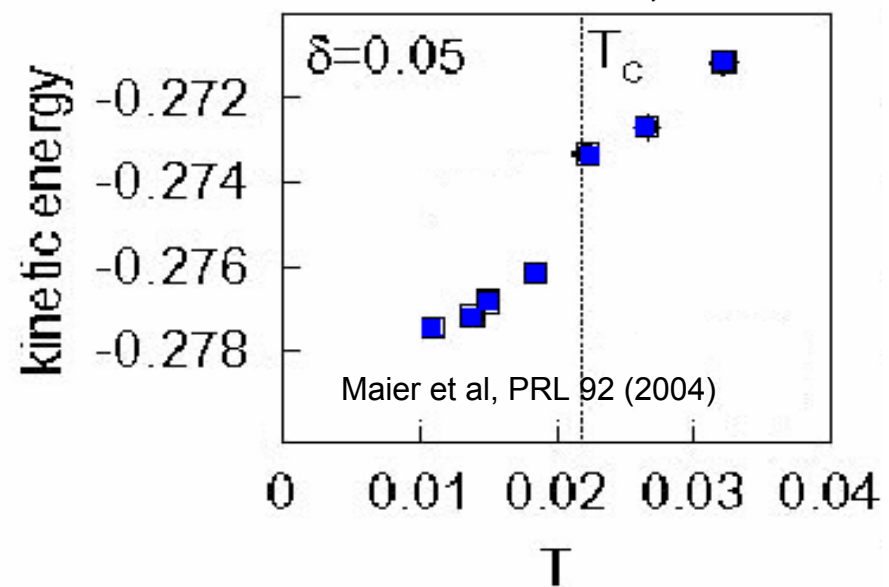
- ▶ The pairing mechanism and kinetic energy
- ▶ Some relevant details of our experimental methods & equipment
- ▶ Spectral weight transfer of the superconducting state
- ▶ The relevant energy scales of optical SW transfer
- ▶ Doping dependence of the SW transfer

# The Pairing mechanism and the electronic Kinetic Energy

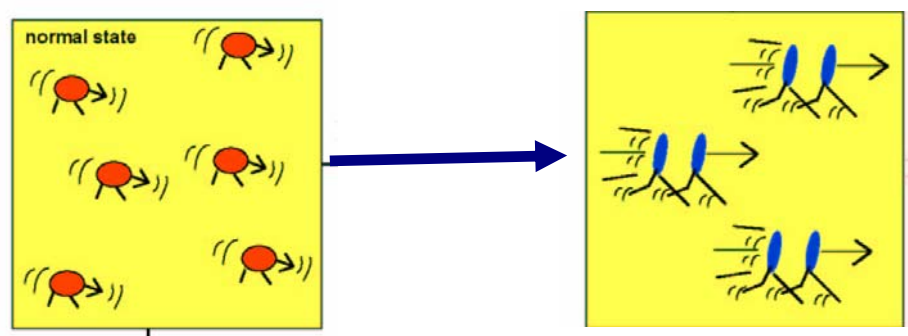
BCS theory



Hubbard model, DMFT



## Theoretical Prediction by Hirsch

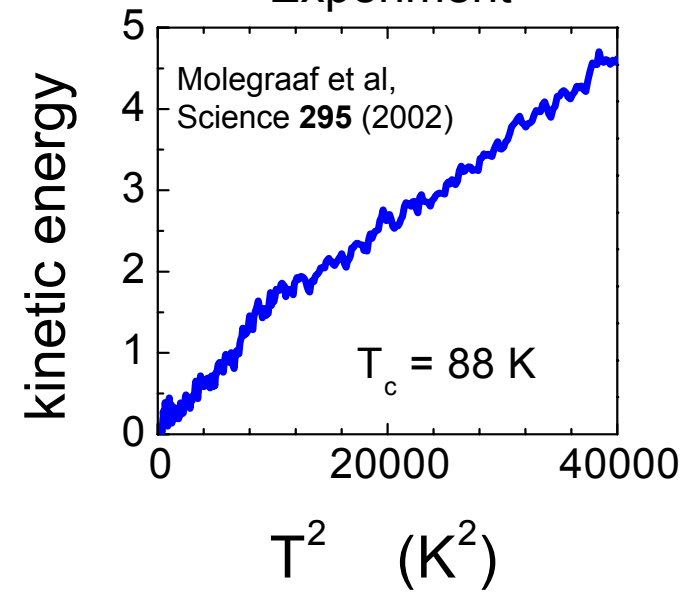


J.E. Hirsch, Physica C **201**, 347 (1992)

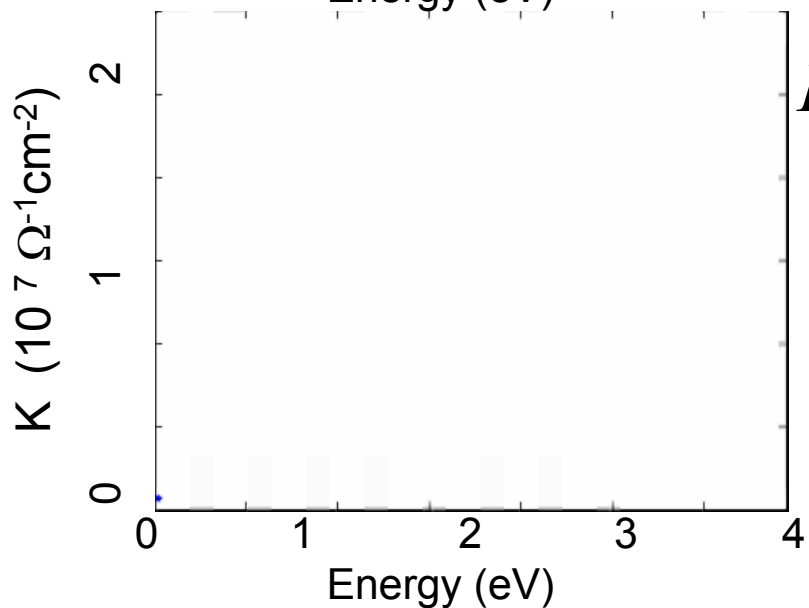
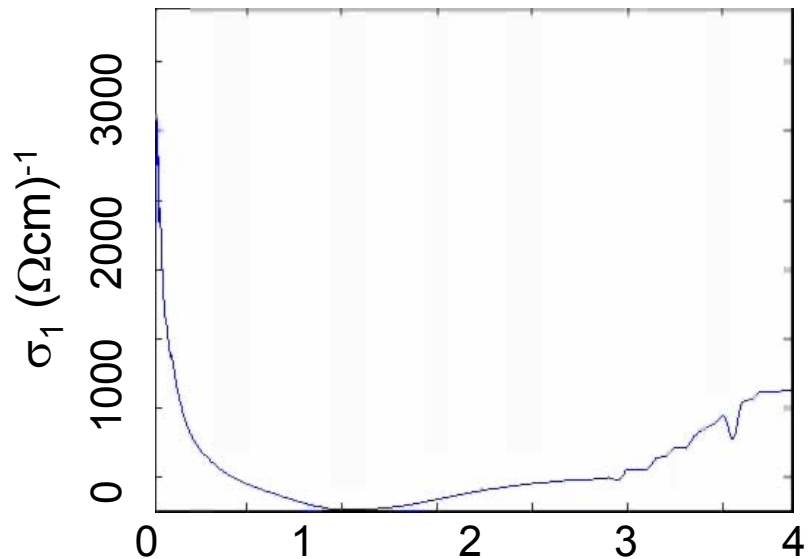
J. E. Hirsch, and F. Marsiglio, Physica C **331** (1999)

J.E. Hirsch, Science **295** (2002).

## Experiment



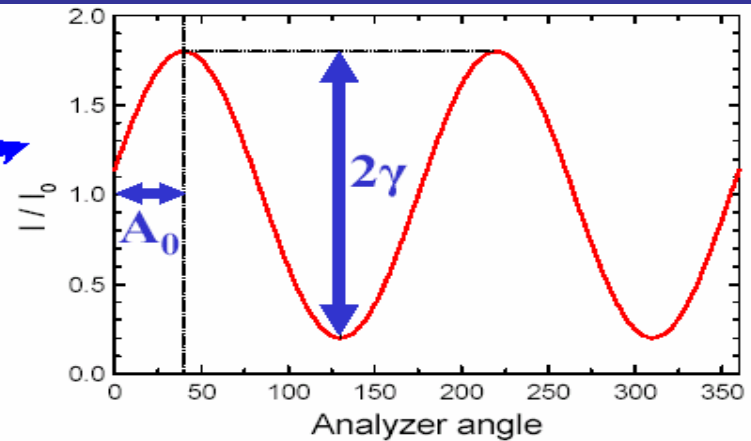
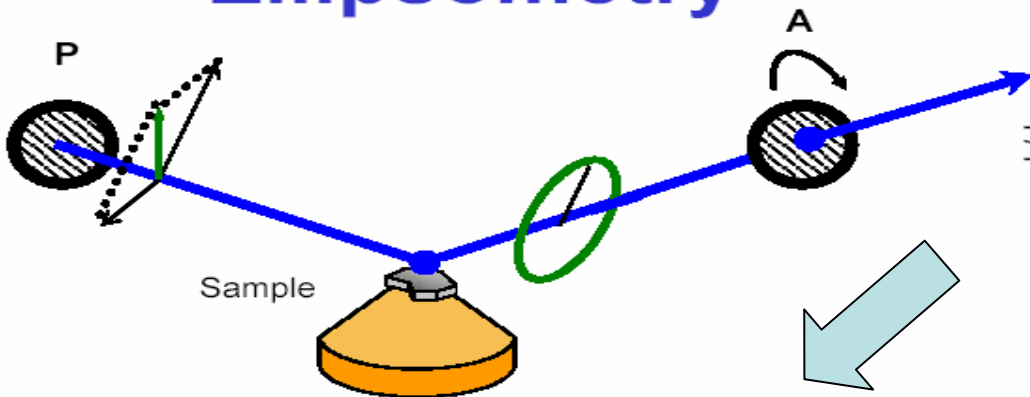
# The SW and the Kinetic Energy



$$K(T) \equiv \frac{2d\hbar^2}{\pi e^2} \int_0^{\Omega_c} \sigma_1(\omega) d\omega = -\langle \hat{H}_{\text{kinetic}} \rangle$$

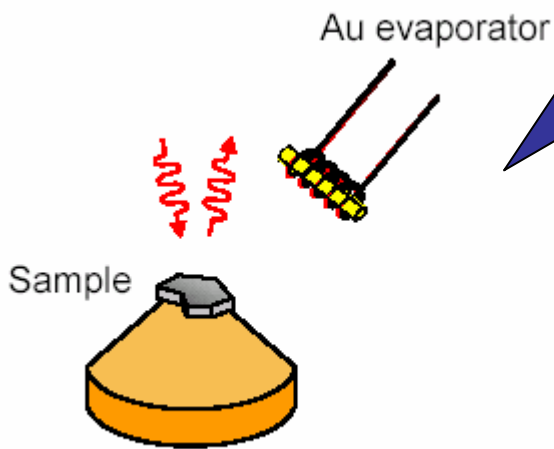
# Experimental determination of $\sigma_1$ $\sigma_2$

## Ellipsometry



$$\varepsilon(\omega) = \varepsilon_1(\omega) + 4\pi i \sigma_1(\omega)/\omega$$

## Reflectivity



Multioscillators variational  
Routine  
Kuzmenko, Rev. Sci. Instr. (2005)



$$\sigma(\omega), \varepsilon(\omega)$$

3d generation optical cryostats:

→ ultra-stable alignment

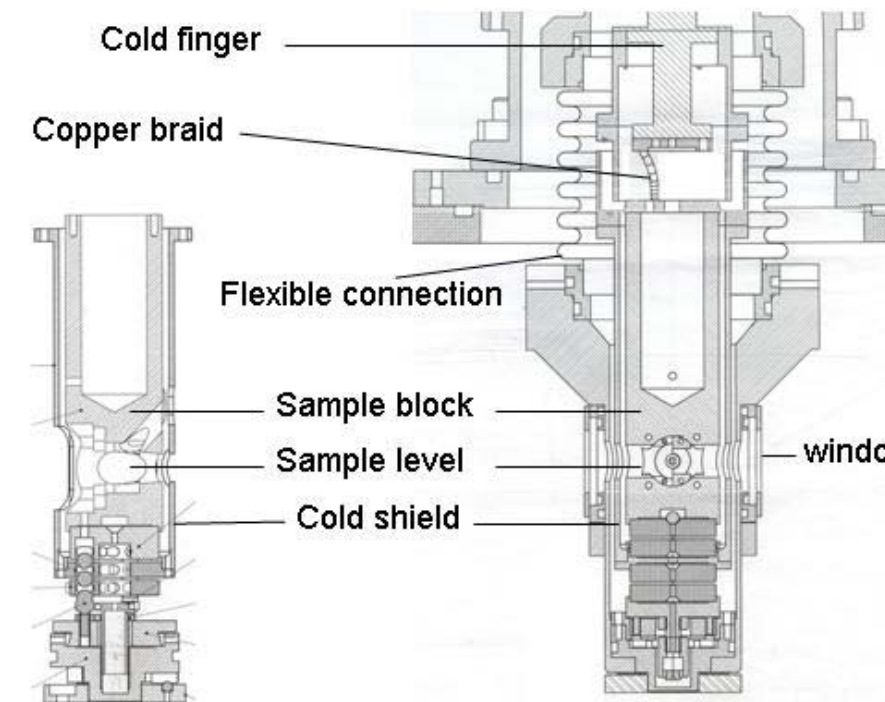
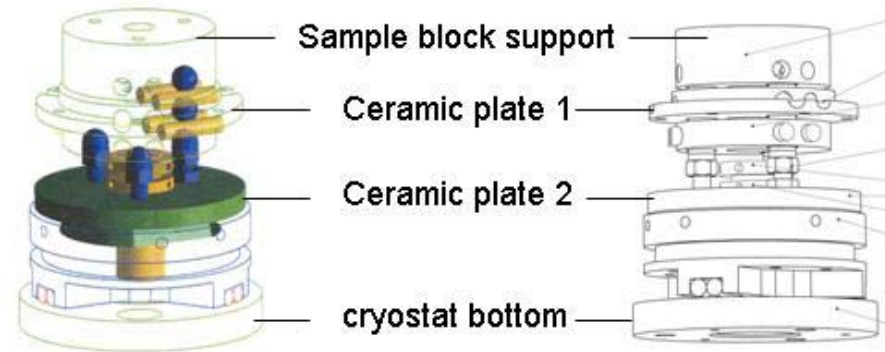
→ signal stability ~0.1 %

→ UH vacuum <  $10^{-9}$  Torr

**Experimental Procedure:**

**1 spectrum/ K**

**4K < T < 300 K**

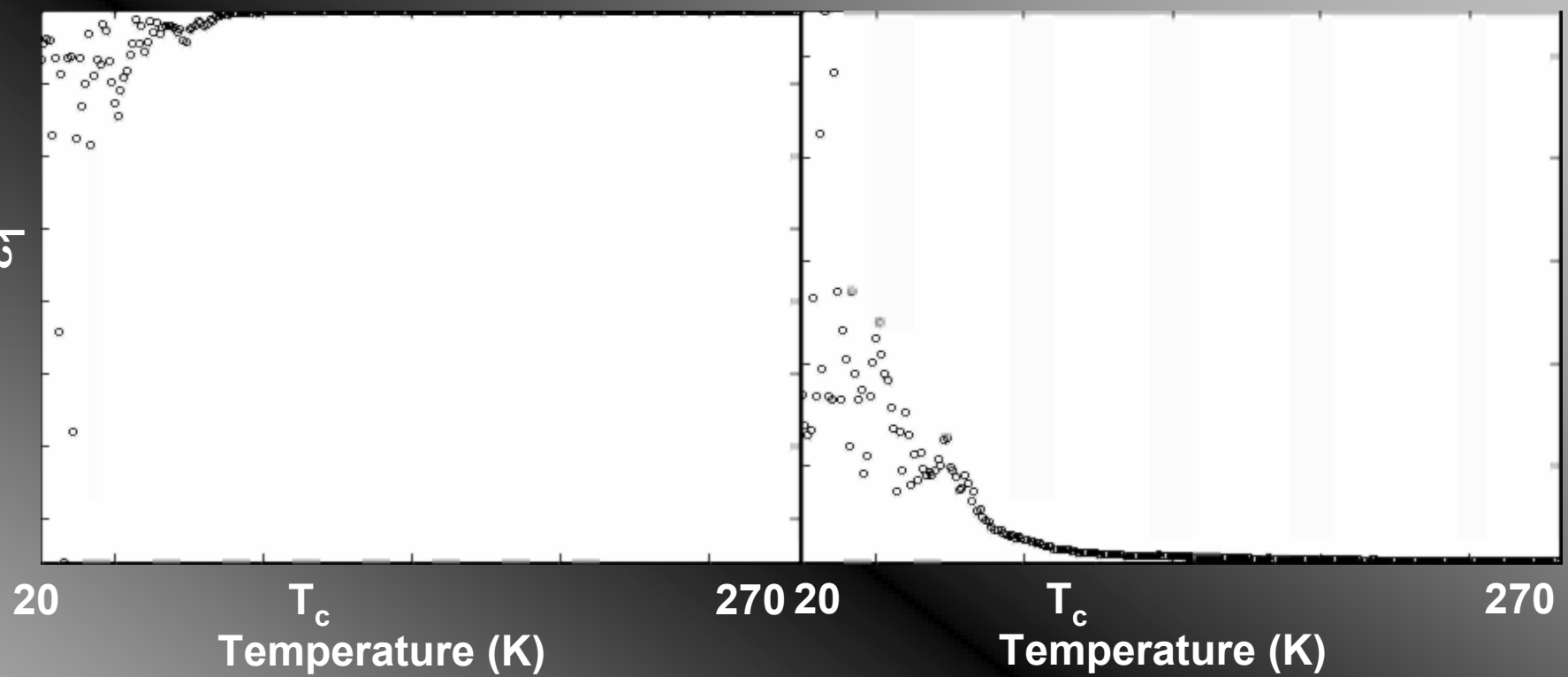


HV cryostat without outer crystal walls

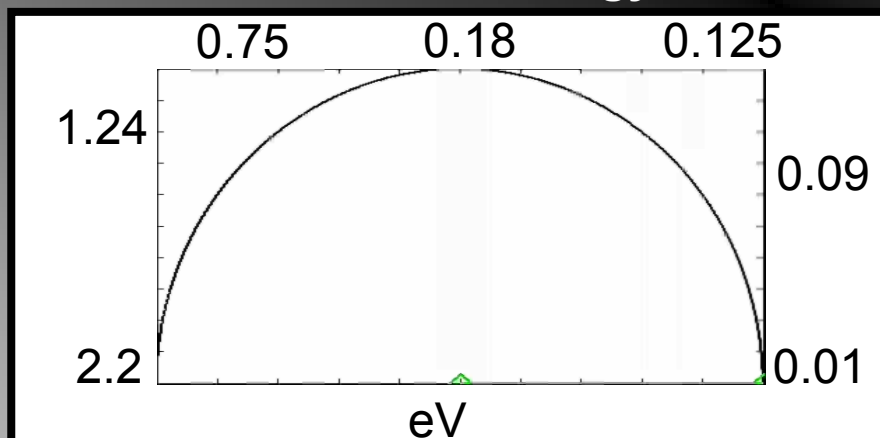
UHV cryostat

►  $E \parallel ab$

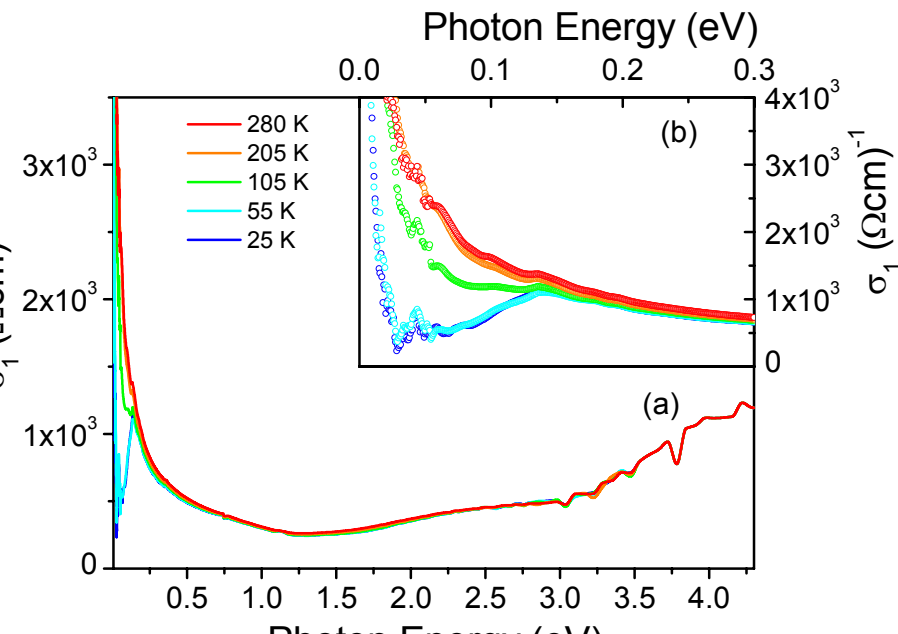
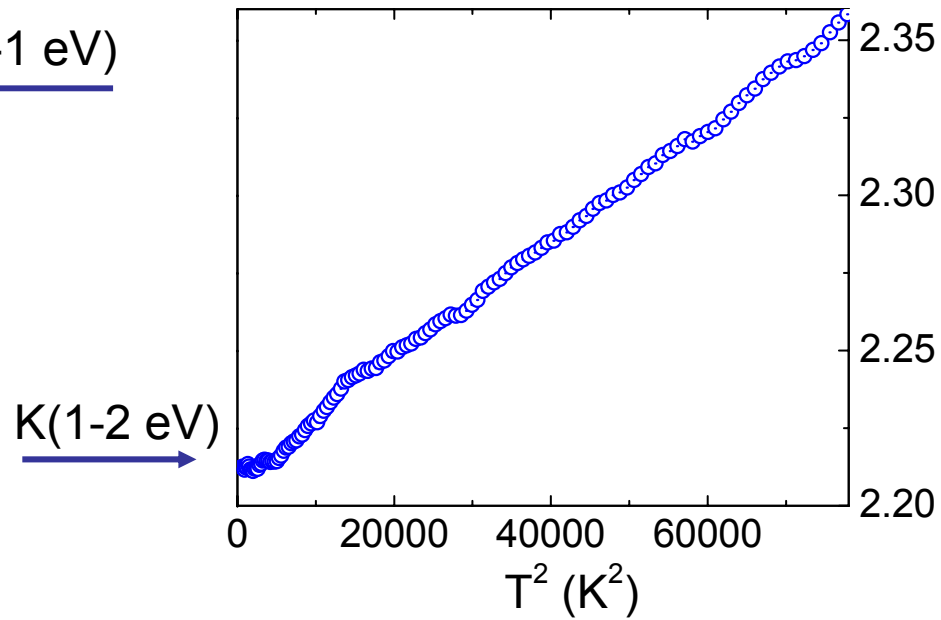
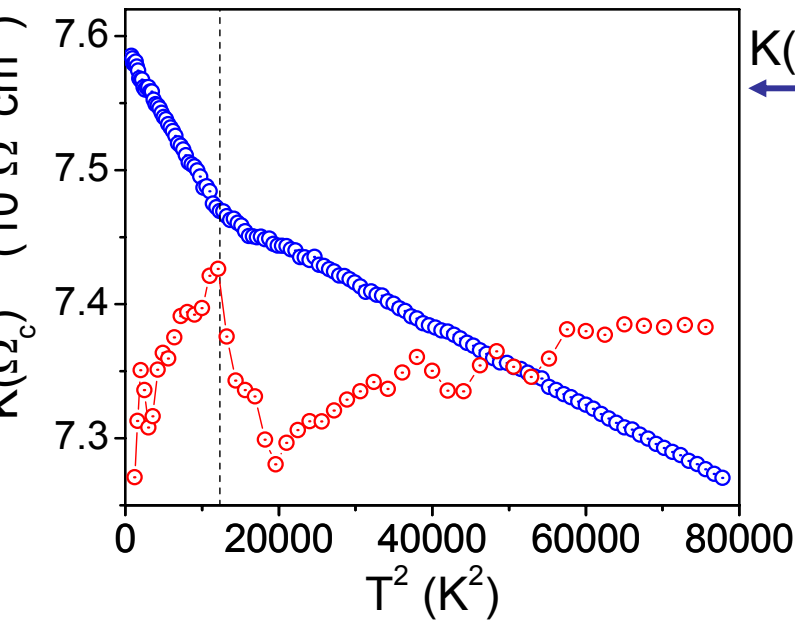
Bi2223  $T_c = 111$  K,  $\sigma_1 \approx \varepsilon_2 * \omega$



Photon Energy



# SW in optimally doped Bi2223, $T_c = 111$ K



$$E \parallel ab$$



**total spectral weight**

$$\frac{2\hbar^2}{\pi e^2} \int_0^\infty \sigma_1(\omega) d\omega = \frac{\hbar^2 n_e}{m_e} = \sum_{k,\sigma} n_{k\sigma} \frac{\hbar^2}{m_e} \quad \text{(f-sum rule)}$$

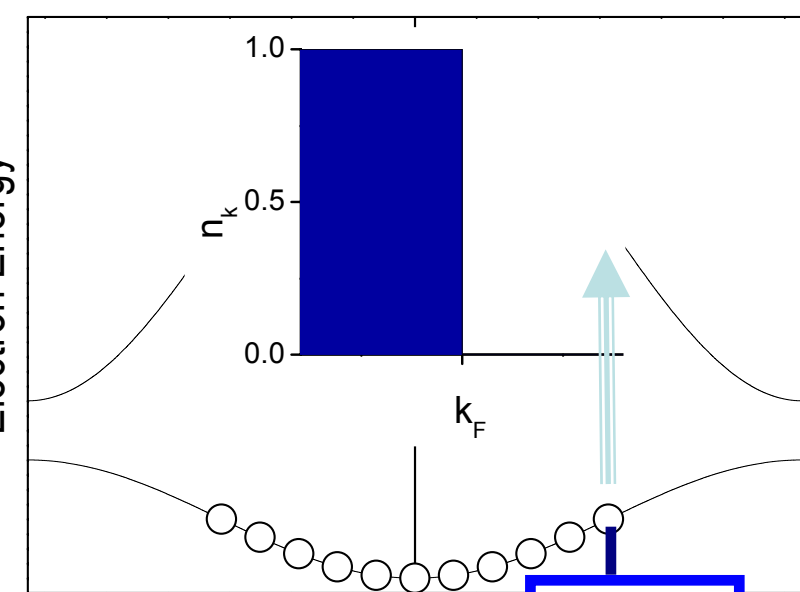
**free charge spectral weight**

$$K \equiv \frac{2d\hbar^2}{\pi e^2} \int_0^{\Omega_c} \sigma_1(\omega) d\omega = \sum_{k,\sigma} n_{k\sigma} \frac{\partial^2 \varepsilon_k}{\partial k^2} \quad \text{(Kubo, 1957)}$$

$= -\langle H_{\text{kinetic}} \rangle$  (exact for nearest neighbor tightbinding)

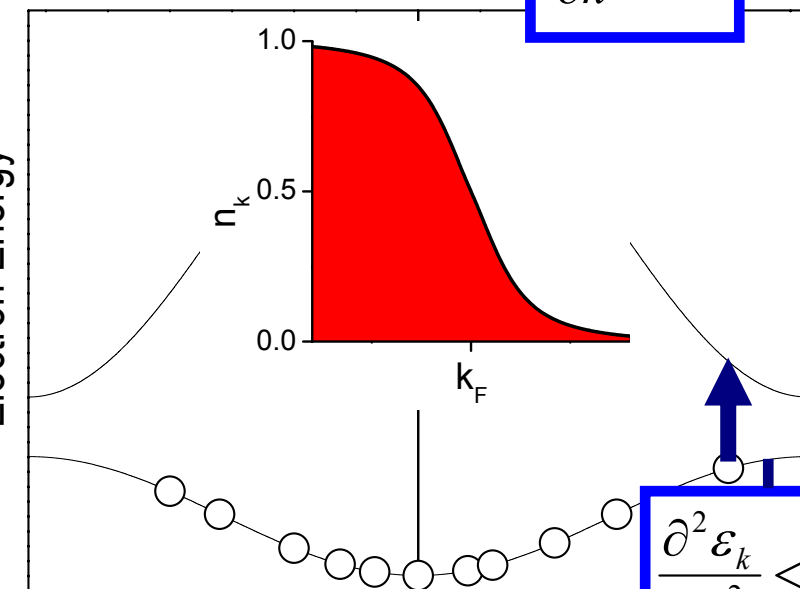
**bound charge (inter-band) spectral weight**

$$\frac{2\hbar^2}{\pi e^2} \int_{\Omega_c}^\infty \sigma_1(\omega) d\omega = \frac{\hbar^2 n_e}{m_e} - K = \sum_{k,\sigma} n_{k\sigma} \left\{ \frac{\hbar^2}{m_e} - \frac{\partial^2 \varepsilon_k}{\partial k^2} \right\}$$

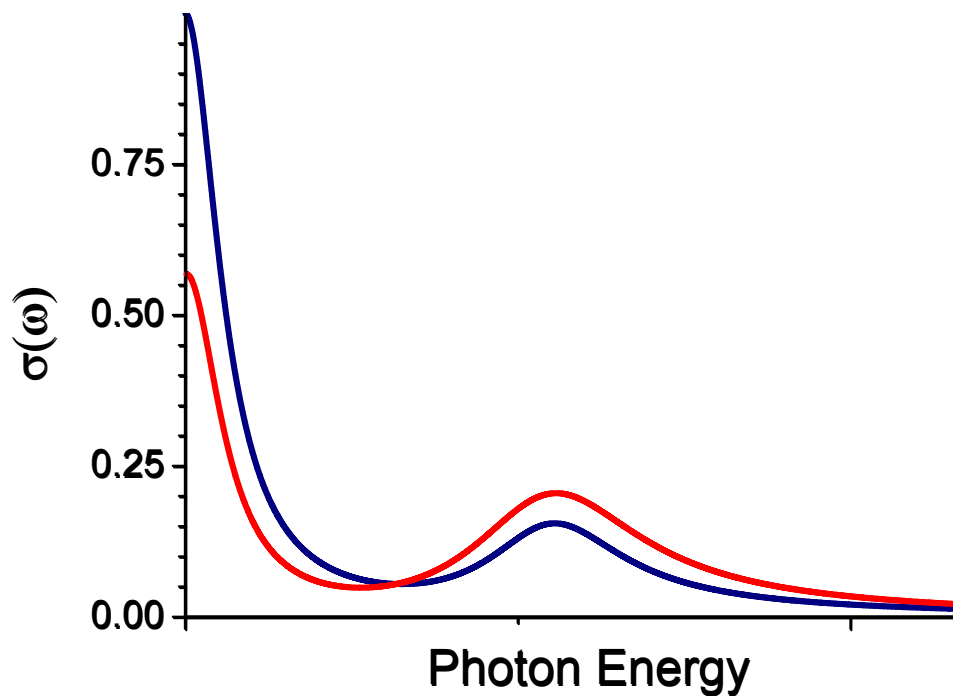


Electron Momen

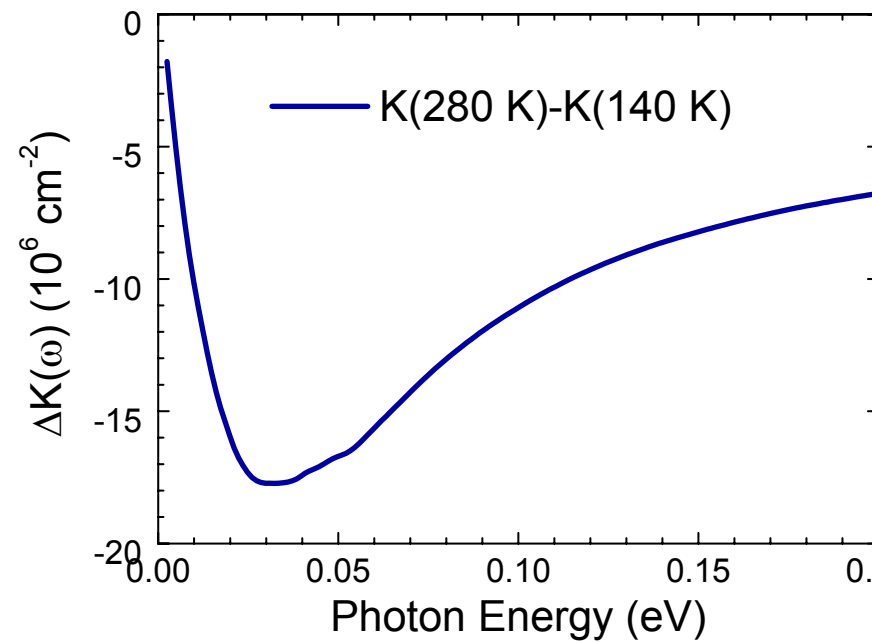
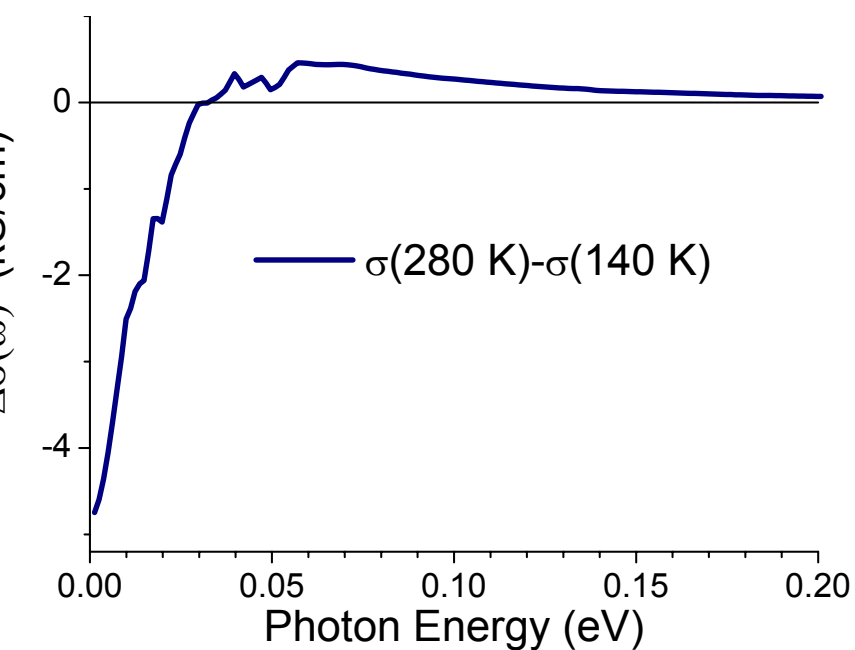
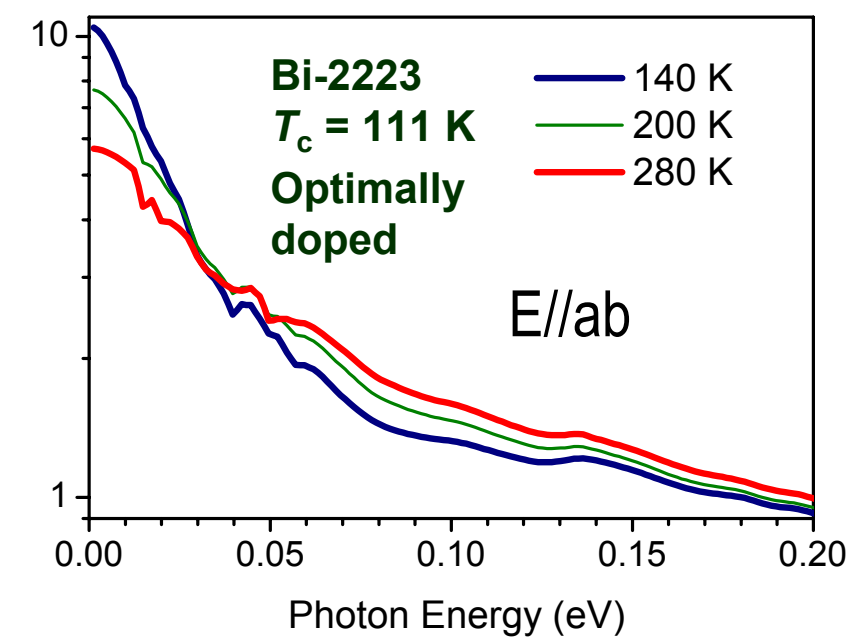
$$\frac{\partial^2 \epsilon_k}{\partial k^2} = 0$$



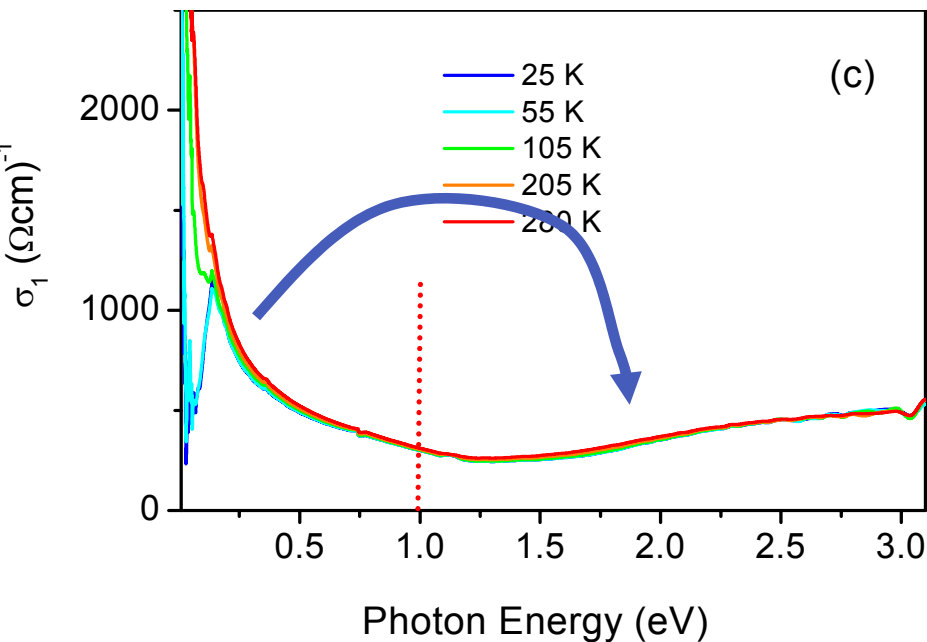
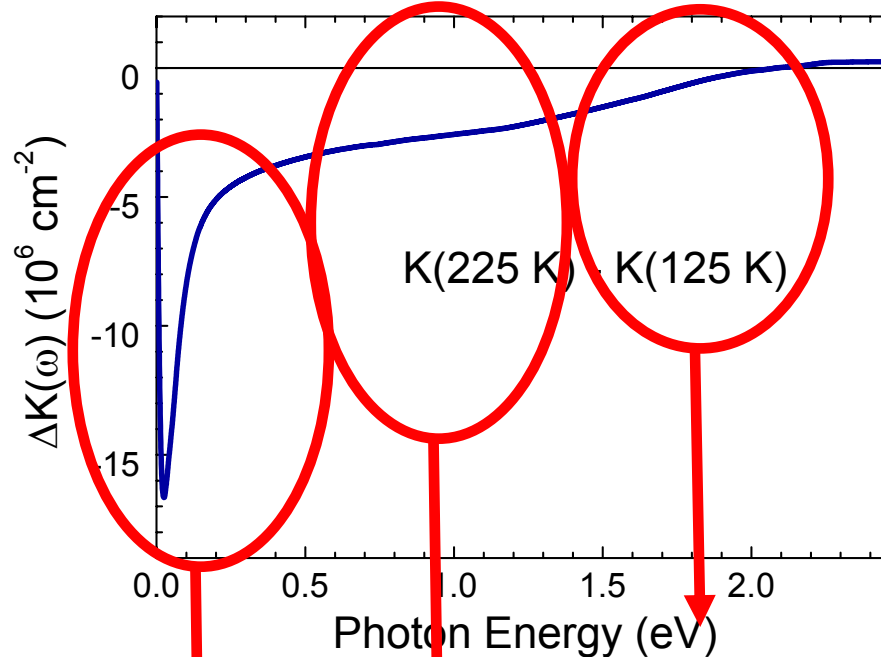
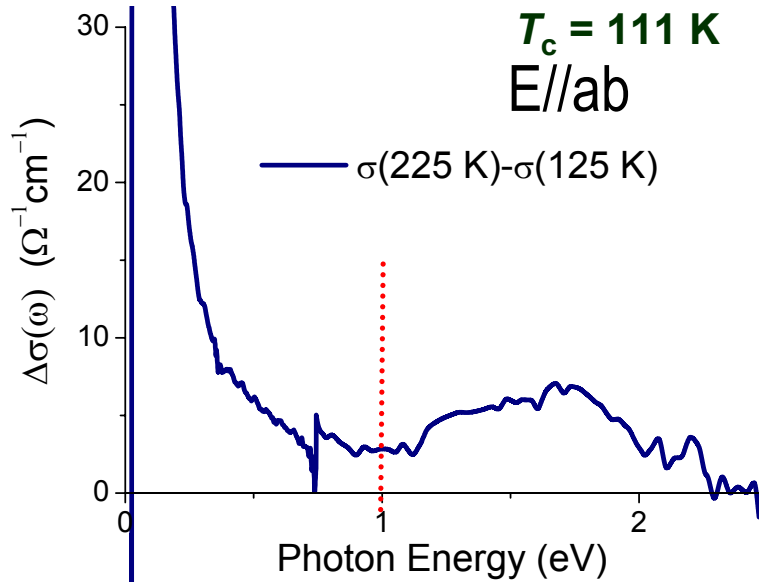
$$\frac{\partial^2 \epsilon_k}{\partial k^2} < 0$$



-K(T) and  $\langle H_{\text{kin}} \rangle_T$  follow the same trend  
 -exceptions are possible



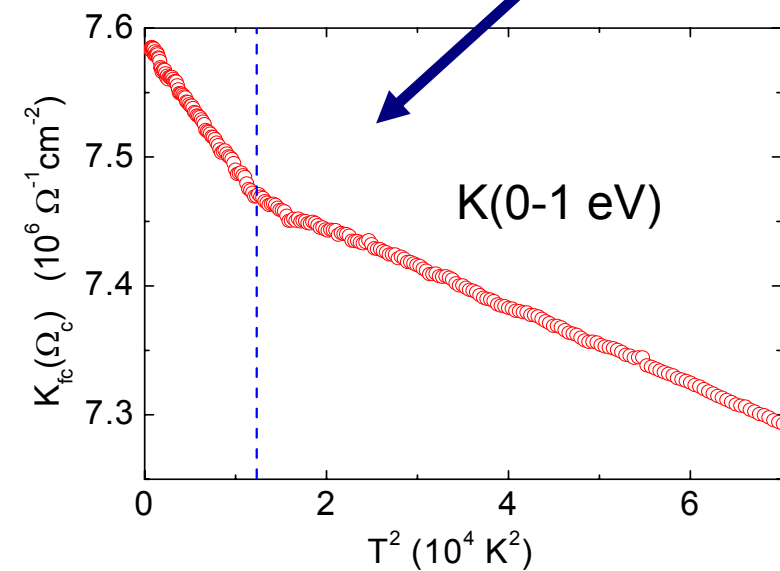
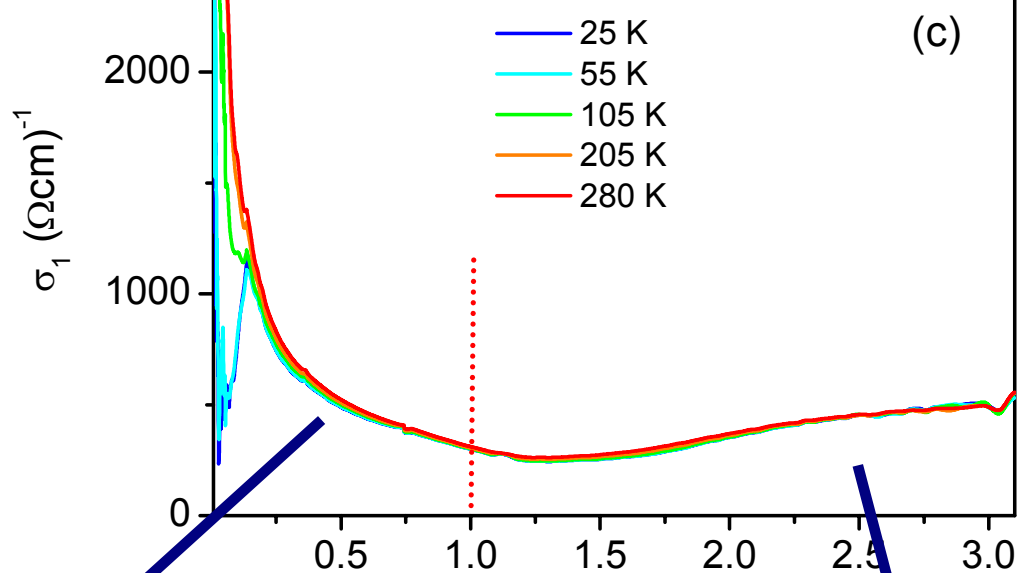
Bi-2223  
 $T_c = 111$  K  
E//ab



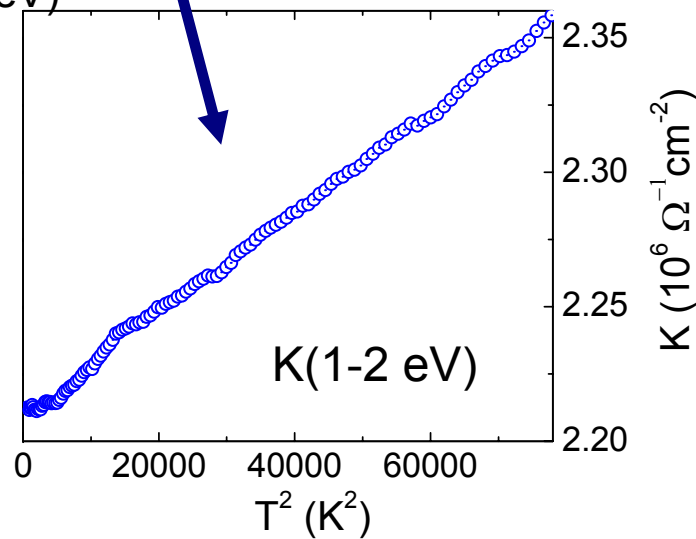
Spectral weight recovery  
Spectral weight deficit  
Drude broadening

Wrobel, Eder, Fulde, JPC 15 (2003):  
 $0.125 \text{ eV} \sim J < \Omega_c < t \sim 0.4 \text{ eV}$   
should provide kinetic energy in t-J mode

**Bi-2223**  
 **$T_c = 111$  K**  
 **$E//ab$**



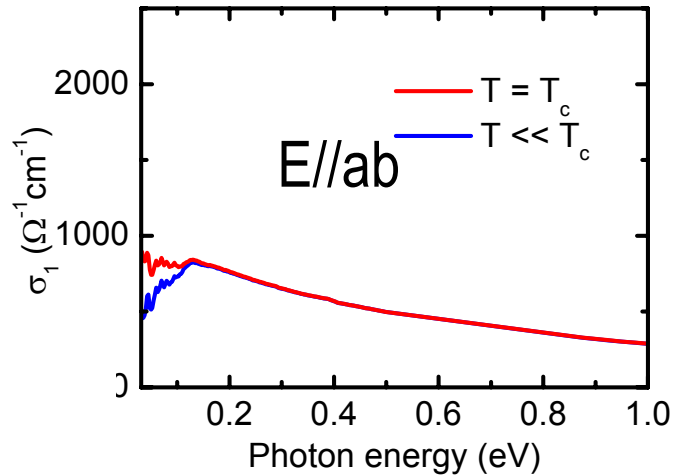
Photon Energy (eV)



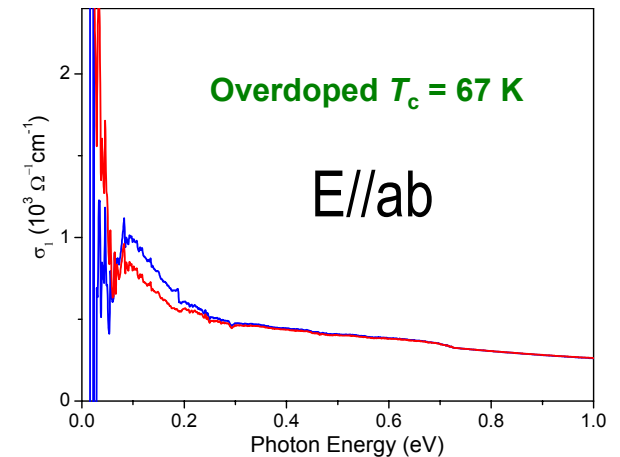
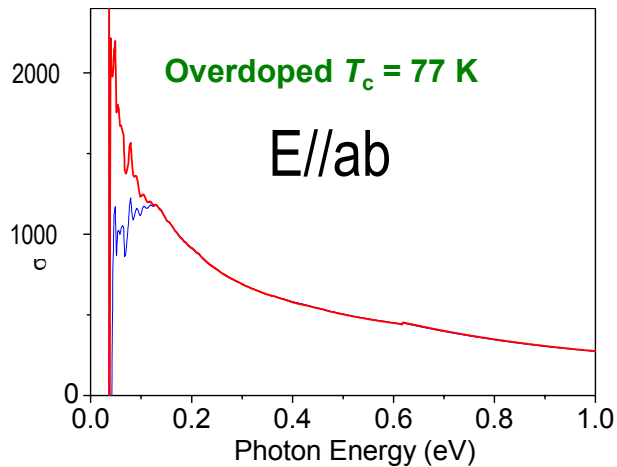
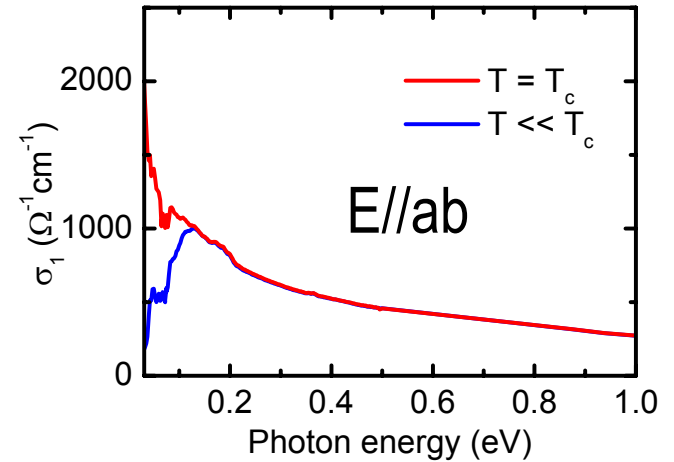
$$K_{fc}(T)_{\text{exp}} / K_0 = 1 - \eta (k_B T / K_0)^2 + \dots$$

# Bi-2212: doping dependence

Underdoped  $T_c = 66$  K



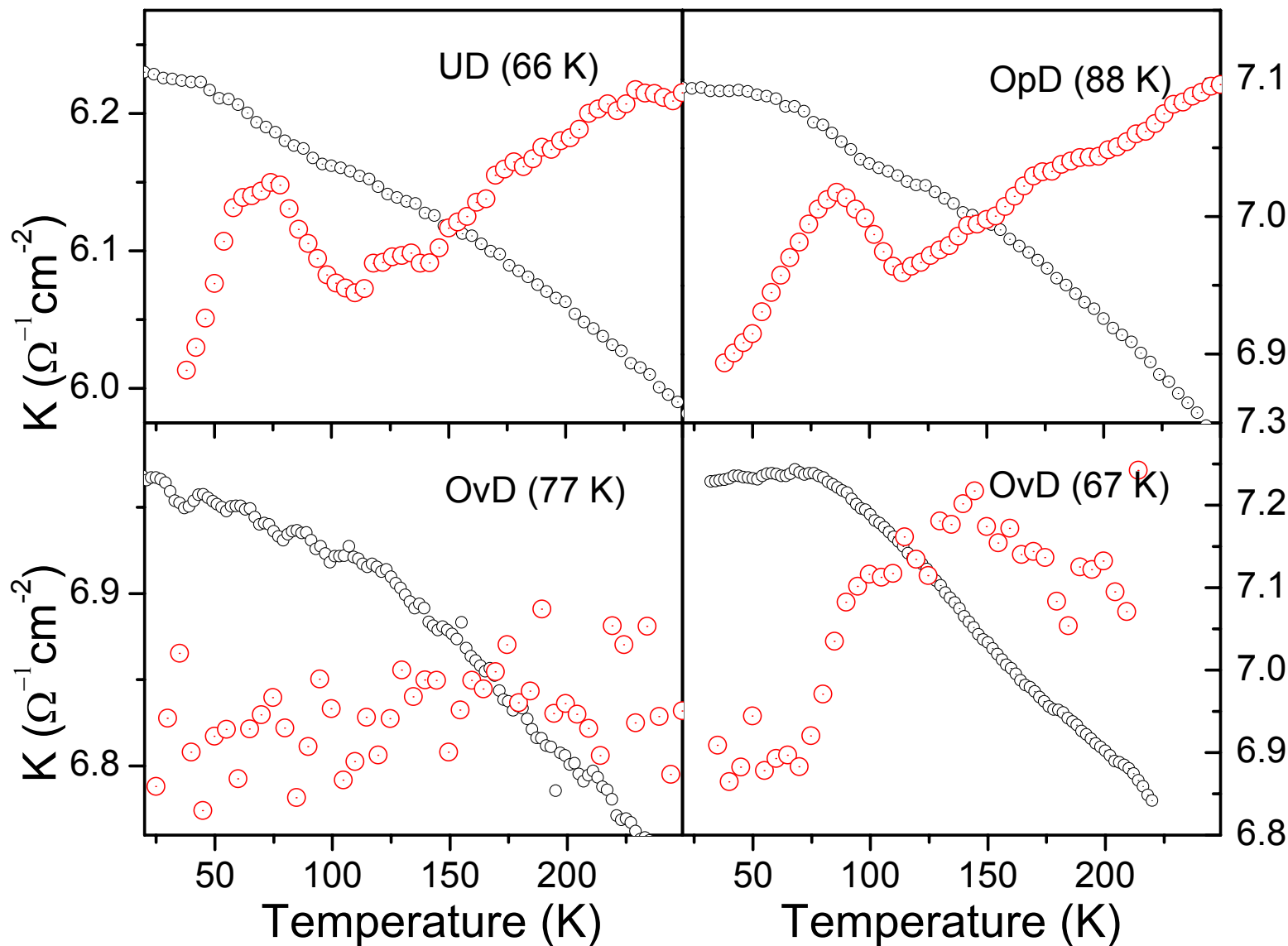
Opt. doped  $T_c = 88$  K

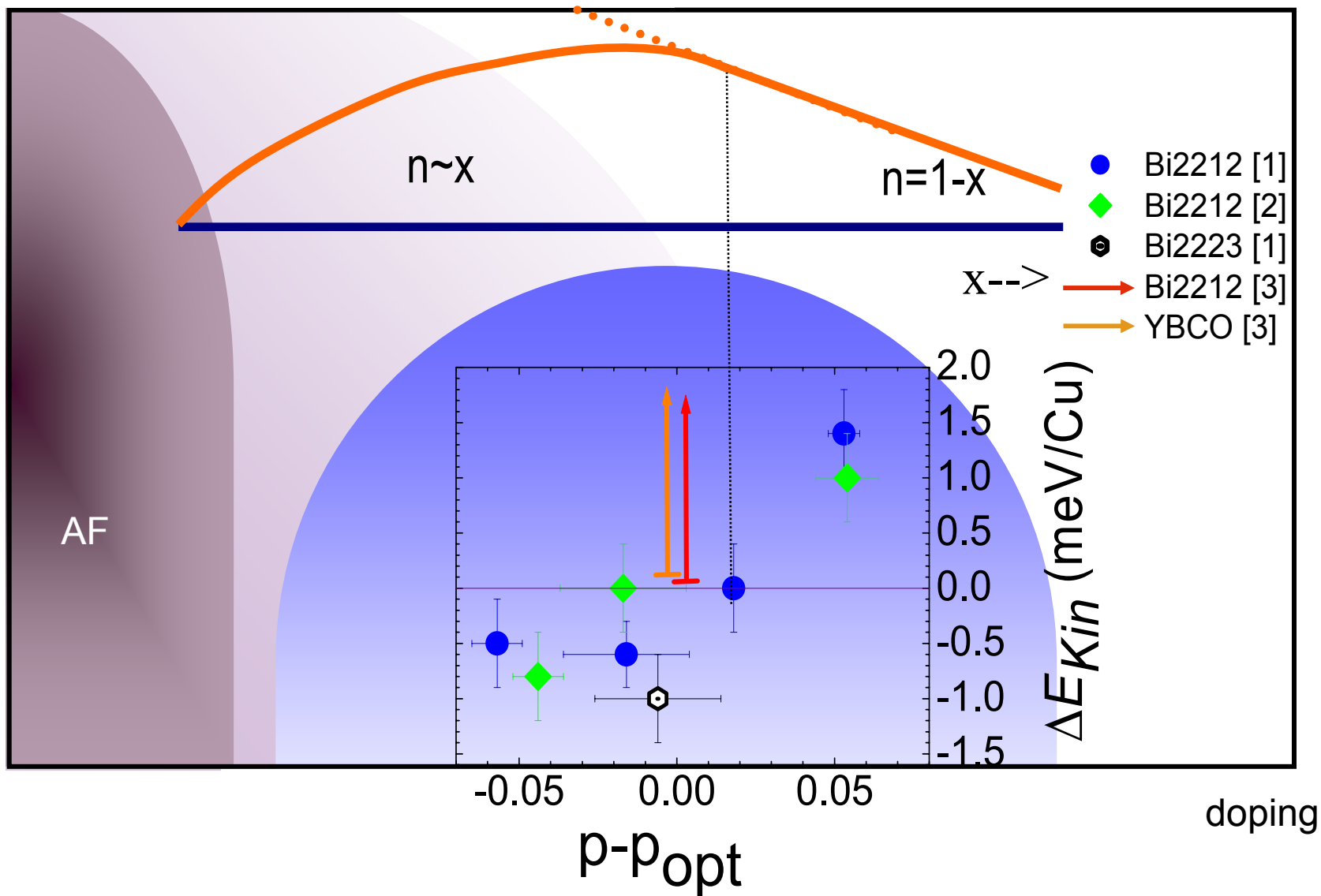


H.J.A.Molegraaf *et al*, Science **295**, 2239 (2002)  
A.B.Kuzmenko *et al*, cond-mat/0503768, subm. to PRB

F. Carbone *et al*, to be published,

# The doping dependence of the SW in Bi2212





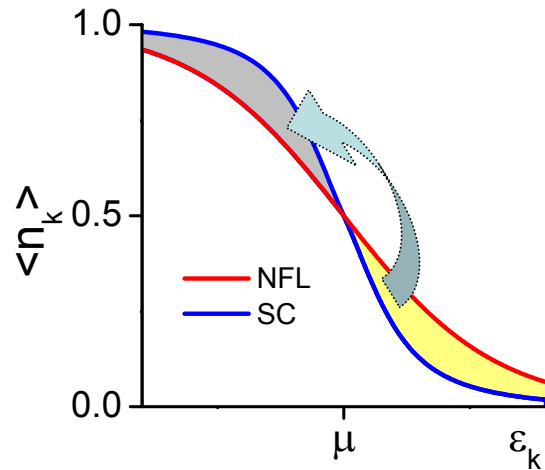
[1] Molegraaf et al, Science 295, 2239 (2002), Carbone et al, submitted to Phys. Rev. Lett. (2005)

[2] Santander-Syro et al, Europhys. Lett 62, 568 (2003), Deutscher et al cond-mat 0503073



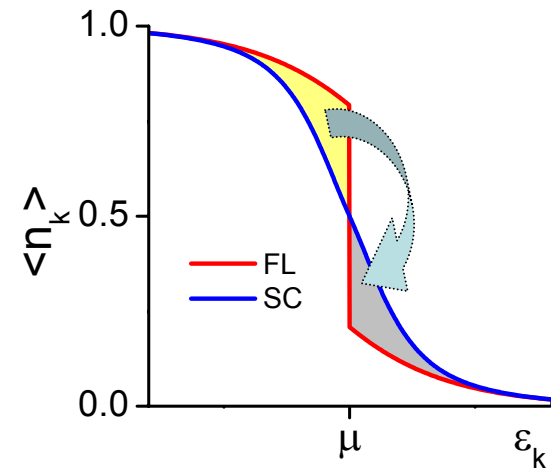
# SC-induced change of $\langle n_k \rangle$

**Non-FL scenario  
(kinetic energy lowering)**



Superconducting state  
more normal than the  
normal state

**Fermi-liquid BCS scenario  
(potential energy lowering)**



Normal state more normal  
than the superconducting  
state

## CONCLUSIONS

The low frequency SW in the optimally and under-doped samples increases, in agreement with the calculations based on the Hubbard and t-J models

The SW redistribution changes sign in the overdoped region

Normal state SW temperature dependence:

$$K_{fc}(T) = K_{fc}(0) - \eta(k_B T)^2 / K_{fc}(0)$$

Strong renormalization of the temperature coefficient

$$\eta_{\text{exp}} \approx 5 * \eta_{\text{non-correlated}}$$